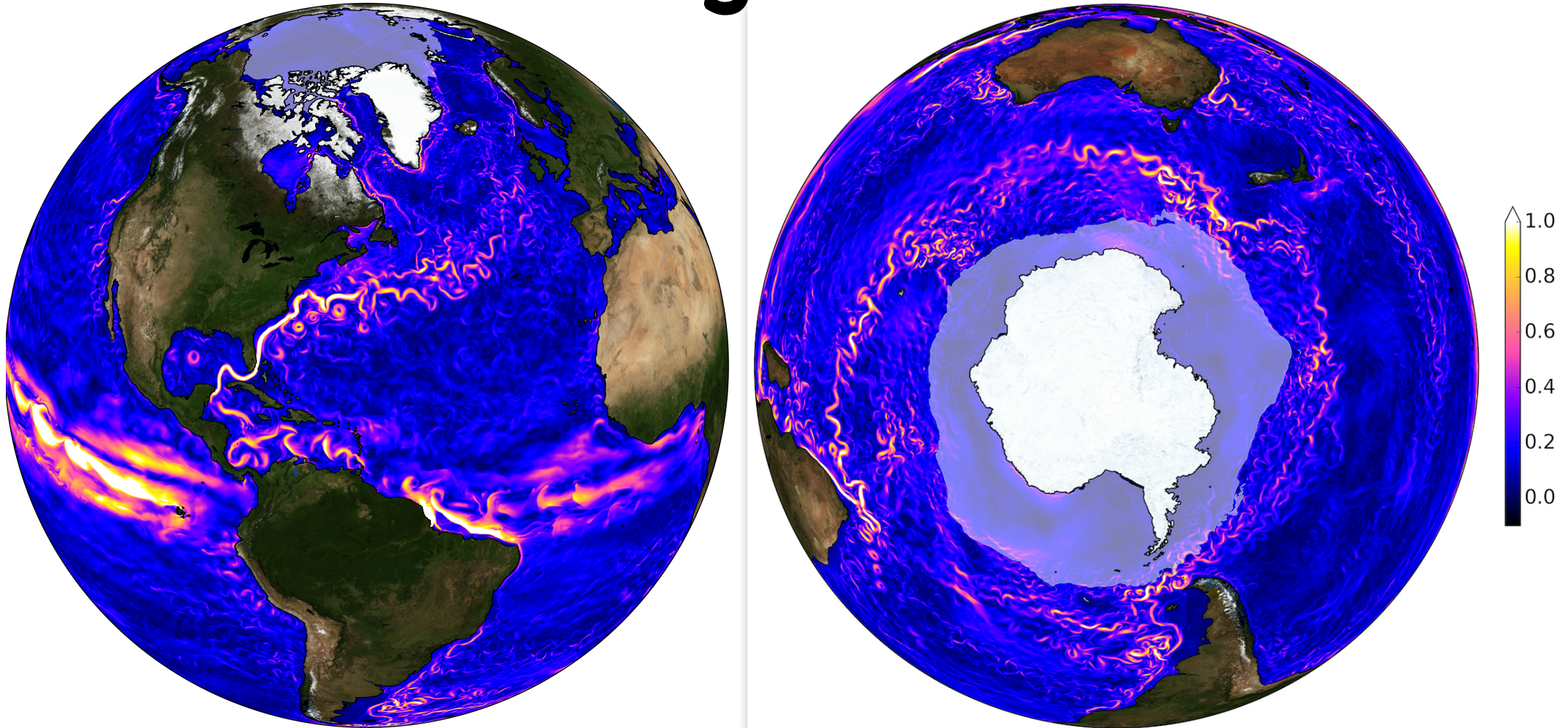


# A Brief Introduction to Modelling the Ocean



Andy Hogg (Australian National University) — with sincere thanks  
to Stephanie Waterman (University of British Columbia)

# What is an ocean model ?

a representation

in the form of

equations / computer code

describing

physical processes

of our understanding of how the ocean works.

# What is an ocean model ?

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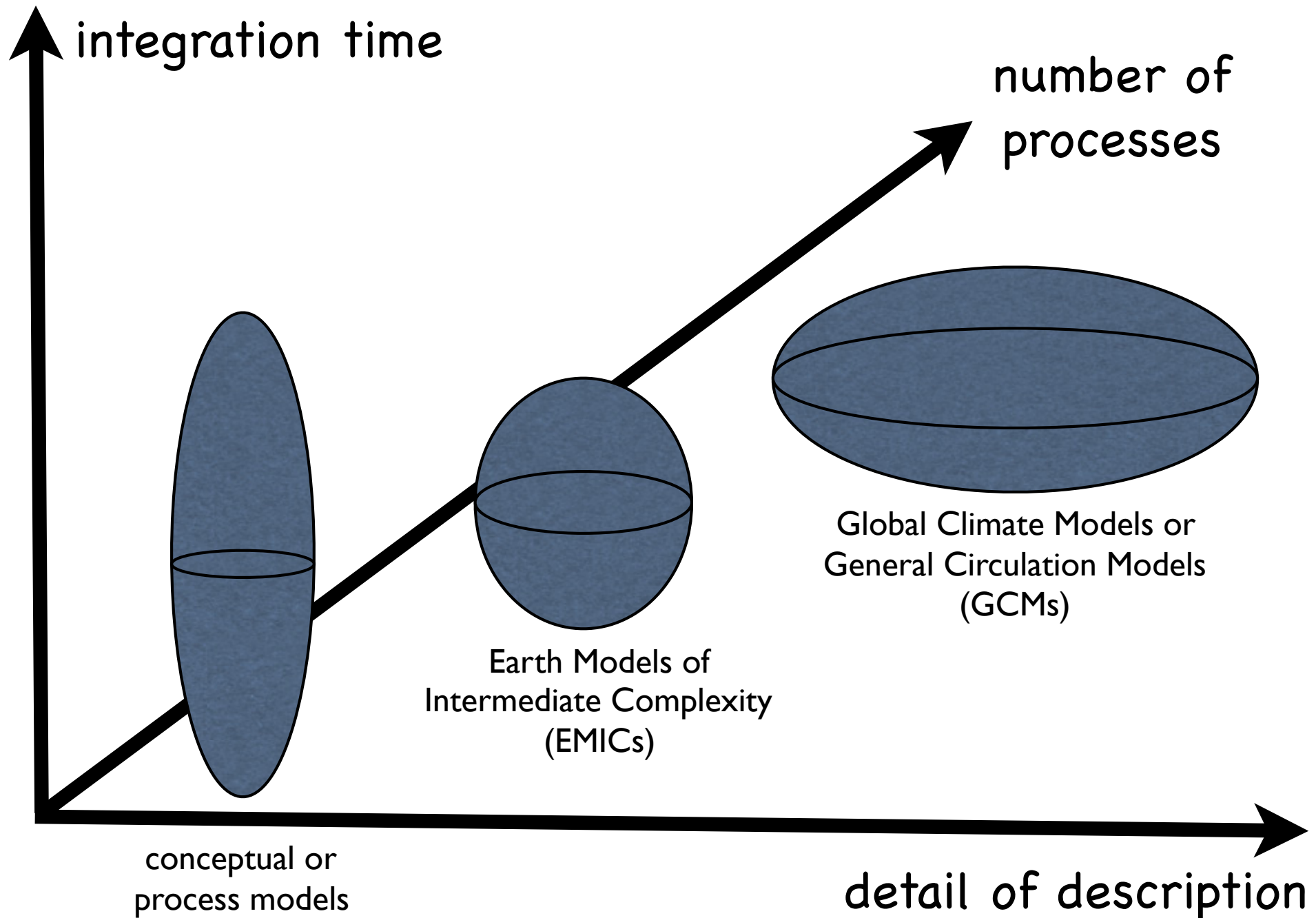
**physical processes**

of our understanding of how the ocean works.



- the exchange of energy, mass, and momentum between the ocean and external sources (e.g. radiation, evaporation, precipitation, river runoff, wind energy that creates waves or currents etc. etc.)
- ocean movement/dynamics including horizontal advection and vertical convection; and
- 3-dimensional mixing and dissipation processes at scales from molecular to ocean basin
- ...

# There are many types of ocean models...

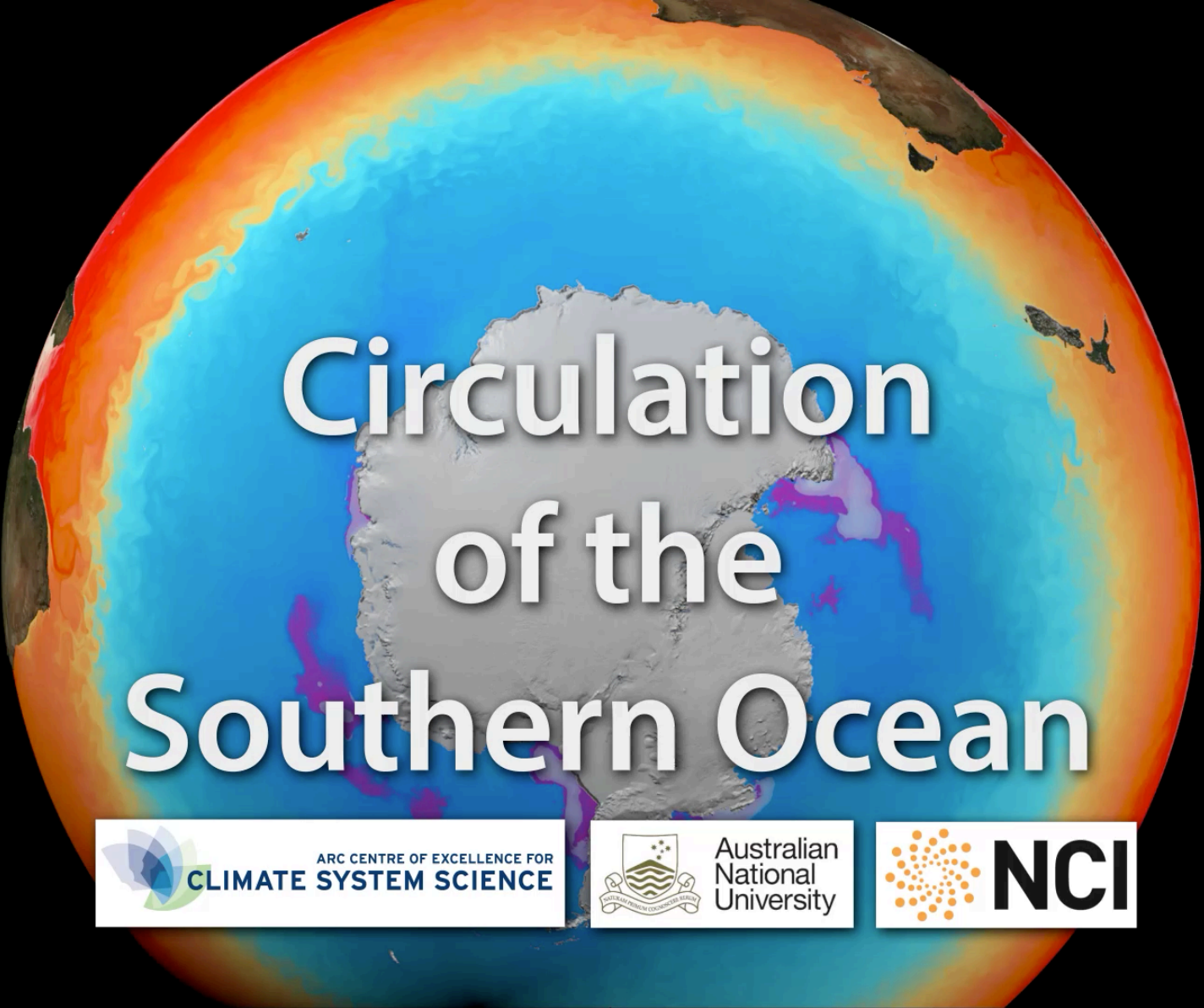




# There are many ways to use ocean models...

- to consider future climate scenarios
- to make operational now-casts and forecasts
- to investigate ocean and climate processes
- to mechanistically interpret ocean observations
- ...

**Remember: All models are wrong, some are useful!**



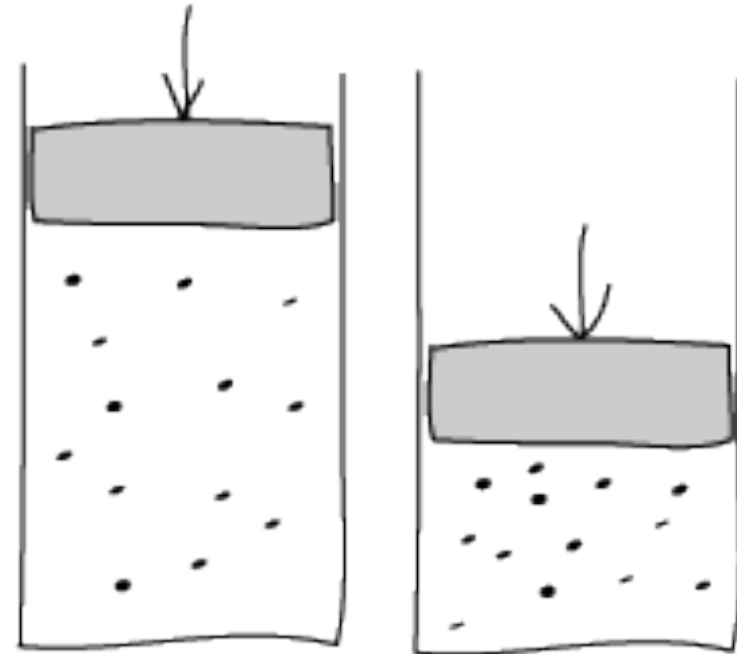
# Circulation of the Southern Ocean



# Ocean vs. Atmospheric Models I

## 1. liquid vs. **gas**

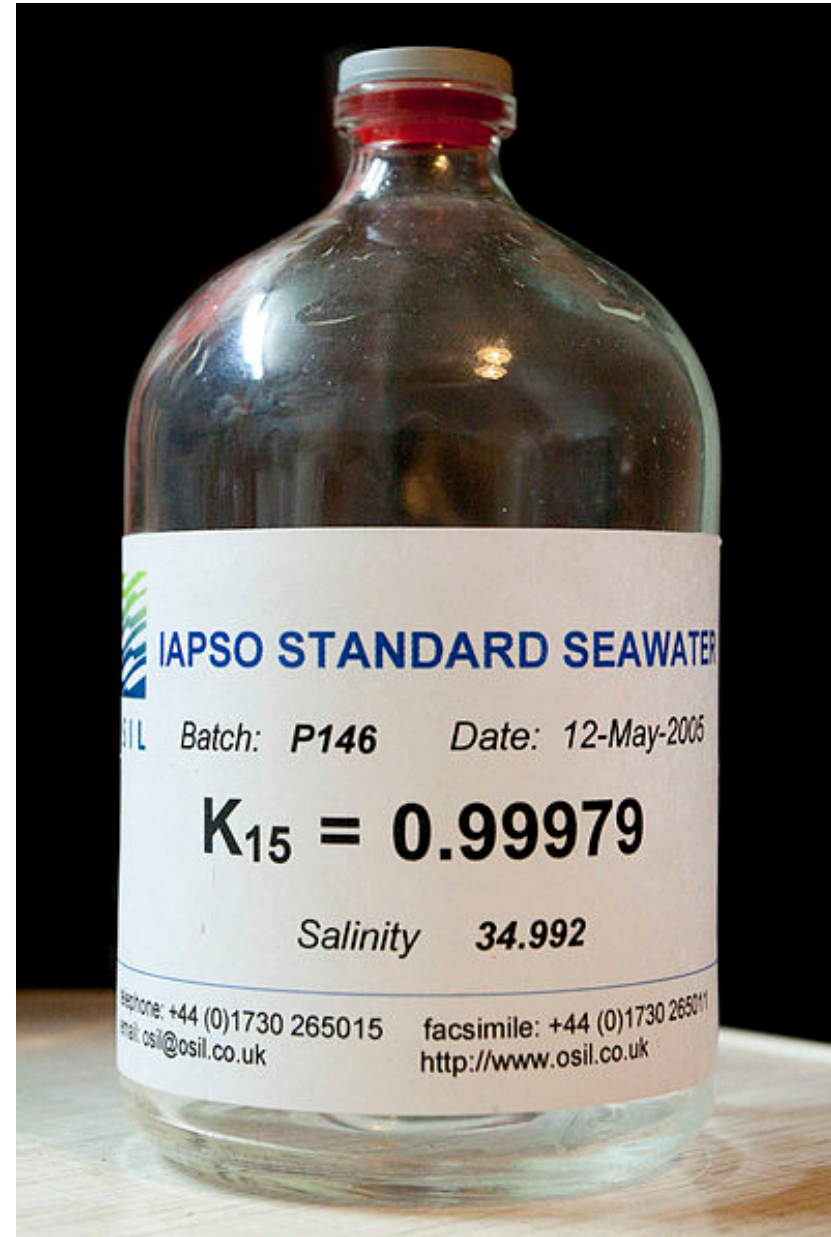
- air is a compressible gas; seawater is a (nearly) incompressible liquid
- this relationship requires a fundamentally different equation of state:
  - atmosphere: ideal gas law (easy!)
  - ocean: density = fn(temperature, salinity, pressure) (hard!)
- **BUT** (in most applications) we can assume incompressibility (so water into a box = water out)



# Ocean vs. Atmospheric Models II

## 2. salinity vs. **humidity**

- seawater contains dissolved chemicals known collectively as “salinity”
- ocean models must account for the effects of salinity on density in an analogous way that atmospheric models must account for humidity

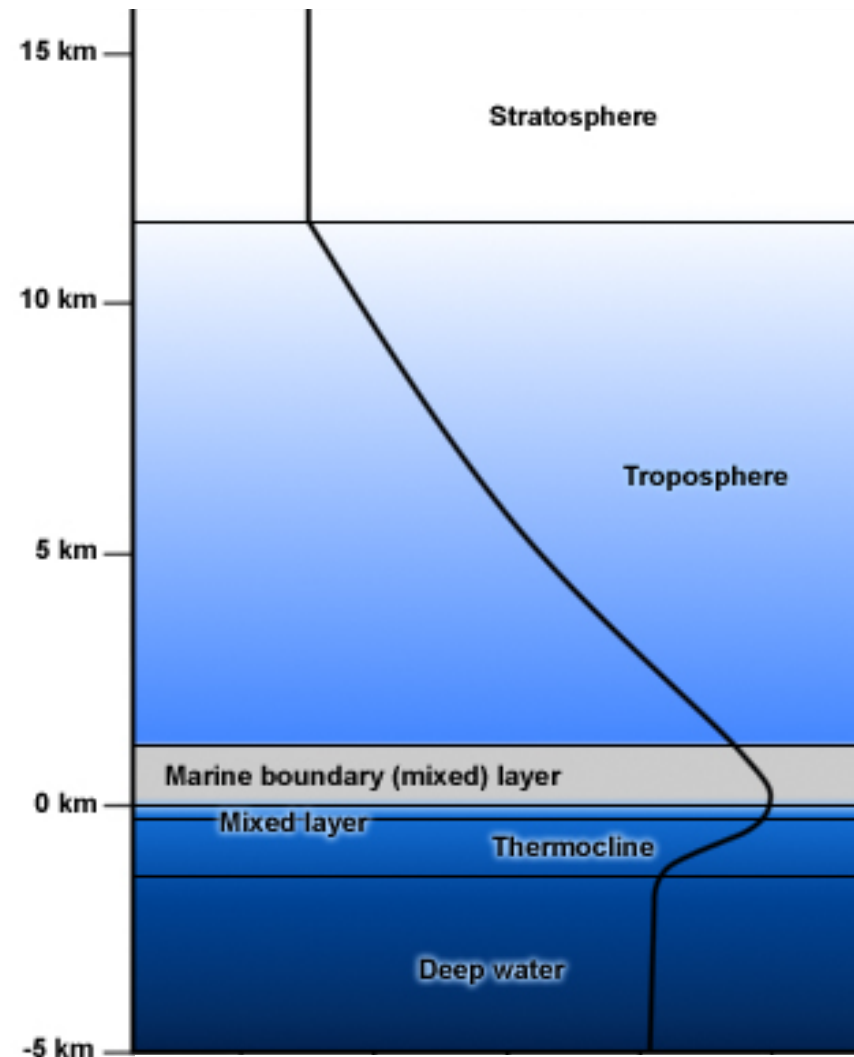




# Ocean vs. Atmospheric Models III

## 3. vertical structure

- the vertical structure of the ocean and atmosphere share both **similarities** and **differences**
- **both have a well-mixed layer near the surface where most of the heating and cooling occurs**
- **BUT** mixing occurs (to some degree) throughout the troposphere while the ocean is stratified below its thin mixed layer
- because the ocean is so stratified, ocean models can make assumptions about the dominance of horizontal processes over those in the vertical
- ocean modellers can benefit from vertical coordinate systems that exploit the fact that much of the action occurs in the near-surface mixed layer



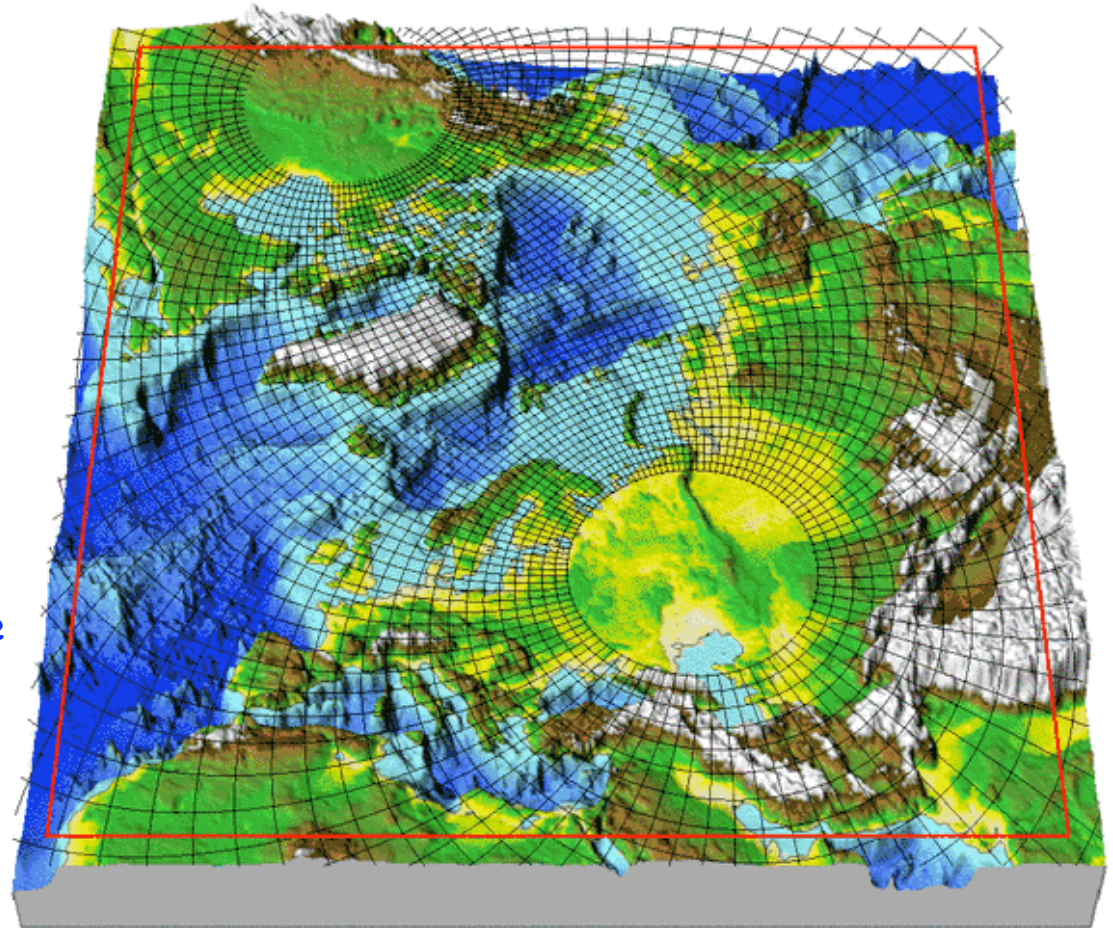
Temperature Profile: Seafloor to Stratosphere

[source: The COMET program]

# Ocean vs. Atmospheric Models IV

## 4. horizontal structure

- the atmosphere blankets the earth in a laterally continuous layer; it is pierced by (relatively) small mountain ranges
- the ocean is bounded on 5 of 6 sides by complex topography:
  - a series of irregularly shaped basins
  - fringed by narrow continental shelves
  - bottom bathymetry plays on  $O(1)$  role
- there are lateral boundary conditions: freshwater run-off from the continents that alters density and currents along the coast
- the need to resolve both horizontal and vertical processes along ocean margins plays a critical role the choice of horizontal and vertical co-ordinate systems

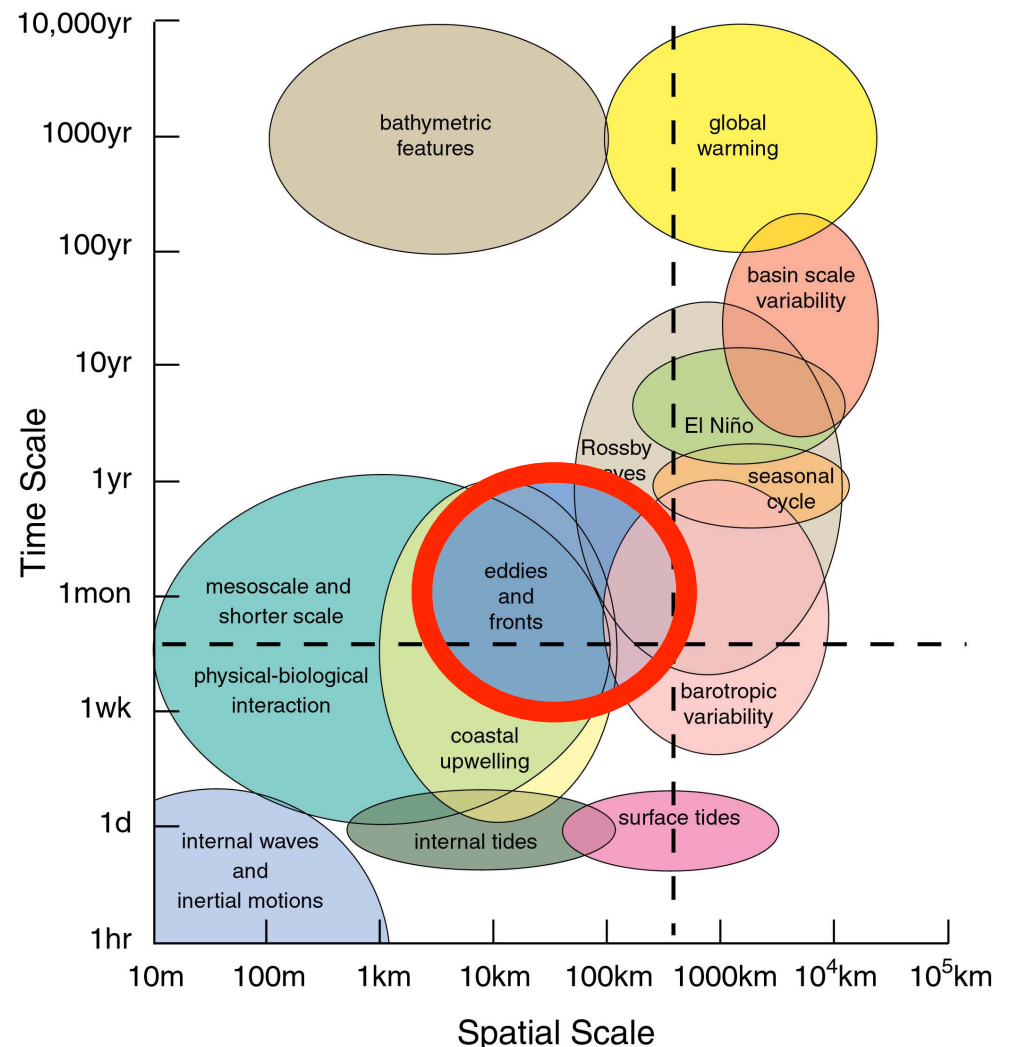


[courtesy of Maxim Nikurashin]

# Ocean vs. Atmospheric Models V

## 5. time and length scales of motion

- Atmospheric models are more expensive than ocean models **for a given grid size**
- **BUT** the energy-containing (geostrophic) scales in the atmosphere are much **larger** than those in the ocean
- this means we need to model the ocean at a finer resolution to resolve the same “types” of features
- also because the ocean interior is almost adiabatic (i.e. along-density surfaces) whereas the atmosphere is (relatively) well-mixed, the **equilibrium timescale** of the ocean is much **s l o w e r**
- to spin up a ocean model from rest: 1000 + years integration !!!



The space and time scales of various ocean phenomena.



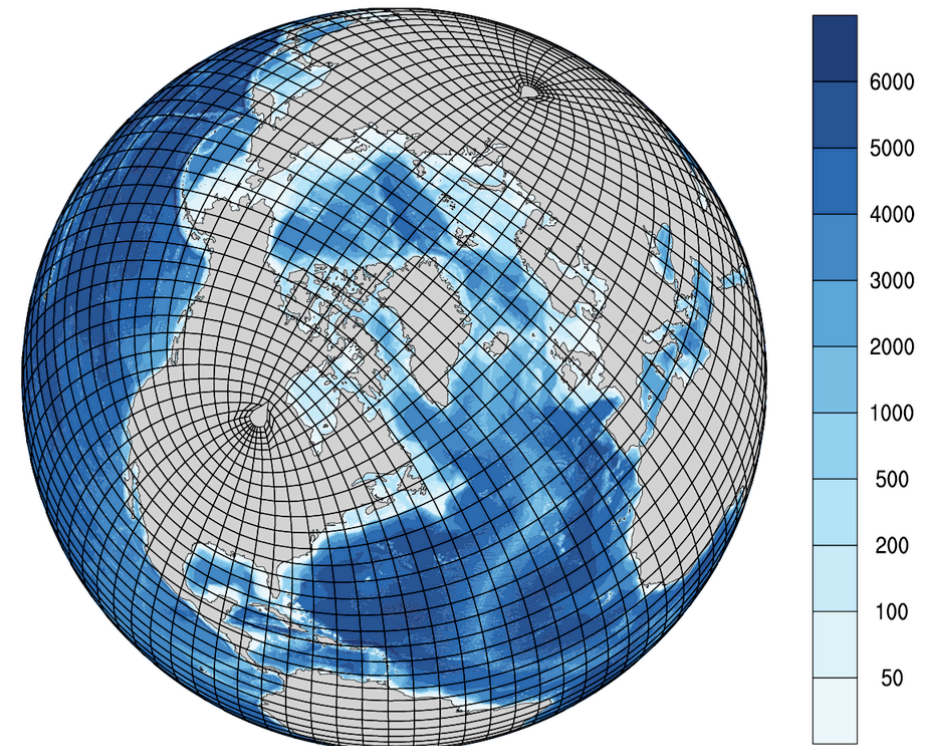
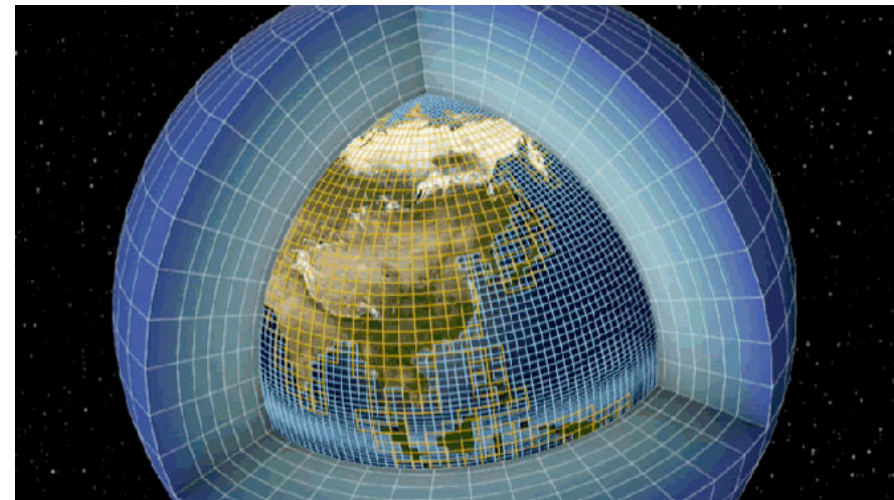
# Ocean vs. Atmospheric Models

Ocean modellers have it both **easy** and **hard** compared to their atmospheric counterparts:

- the ocean is (nearly) incompressible: water in  $\sim$  water out
- the ocean is strongly stratified: horizontal processes dominate over vertical ones
- no change of state of seawater: just form ice when  $T < -1.8^{\circ}\text{C}$

**BUT**

- domain geometry is complex
- lateral boundary conditions are required and poorly constrained
- the eddies are smaller
- the spin-up time is longer
- there are fewer observations for validation





# Ocean Model Ingredients I

## 1. the primitive (hydrostatic) equations

$$\frac{d\vec{u}}{dt} + f\vec{k} \times \vec{u} = -\frac{\nabla P}{\rho} + \vec{F} + \nu \nabla^2 \vec{u}$$

Horizontal momentum

$$\frac{\partial P}{\partial z} = -g\rho$$

Hydrostatic balance

$$\frac{\partial \rho}{\partial t} + \vec{u} \cdot \nabla_H \rho + w \frac{\partial \rho}{\partial z} + \rho \left( \nabla_H \cdot \vec{u} + \frac{\partial w}{\partial z} \right) = 0$$

Conservation of mass

$$\frac{dT}{dt} = \kappa \nabla^2 T + Q_T$$

Conservation of heat

$$\frac{dS}{dt} = \kappa_S \nabla^2 S + Q_S$$

Conservation of salinity

$$\rho = \rho(P, S, T)$$

Nonlinear equation of state

= 7 coupled equations in 7 unknowns:  $u, v, w, P, T, S, \rho$

# Ocean Model Ingredients cont.

## 2. boundary conditions

- basin geometry
- bottom topography
- an atmosphere on top, especially via:

## 3. forcing fields

- shortwave radiation, long-wave radiation, latent heat and sensible heat at the surface
- evaporation and precipitation at the surface
- land surface run-off at the margins
- winds
- tides

## 4. initial conditions (maybe from climatology i.e. the mean state or a previous already spun up model run)

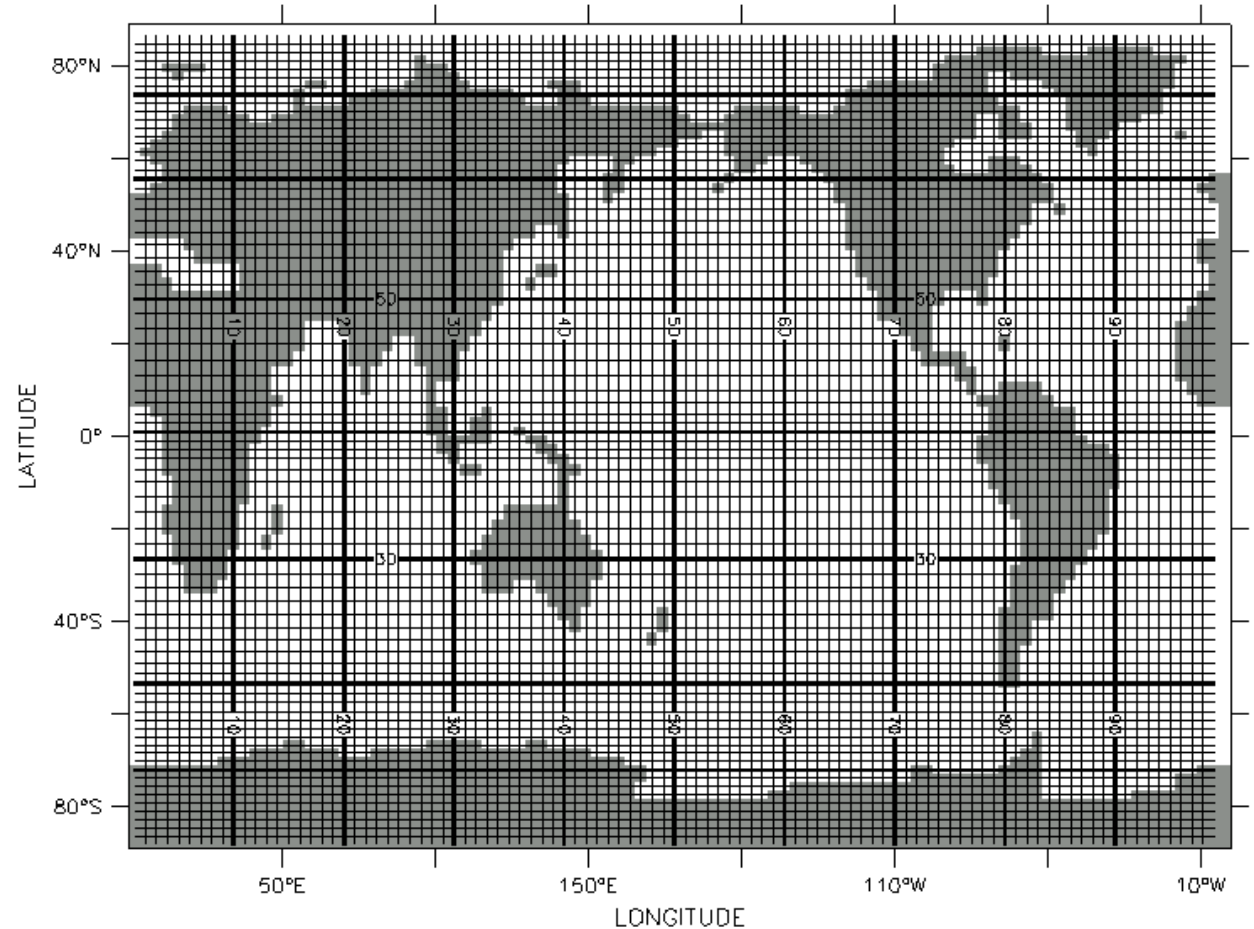
- initial temperature and salinity fields
- initial velocity fields

# Ocean Model Practicalities I

## 1. the horizontal grid

- **regular grids** consist of regularly spaced lines
- on a spherical earth **CAN'T** have both uniform grid spacing **AND** straight lines
- in practice grids tend to be curvilinear and their internal spacing tends to vary
- regular lat-lon grids also have a problem at the poles where grid lines converge

Regular Grid



# Ocean Model Practicalities I

## 1. the horizontal grid

- a clever solution: the **tripolar grid** = a circular grid laid over the Arctic polar region with two poles positioned over land

Tri-polar Grid



[Schopf 2005 after Murray 1996]



# Ocean Model Practicalities I

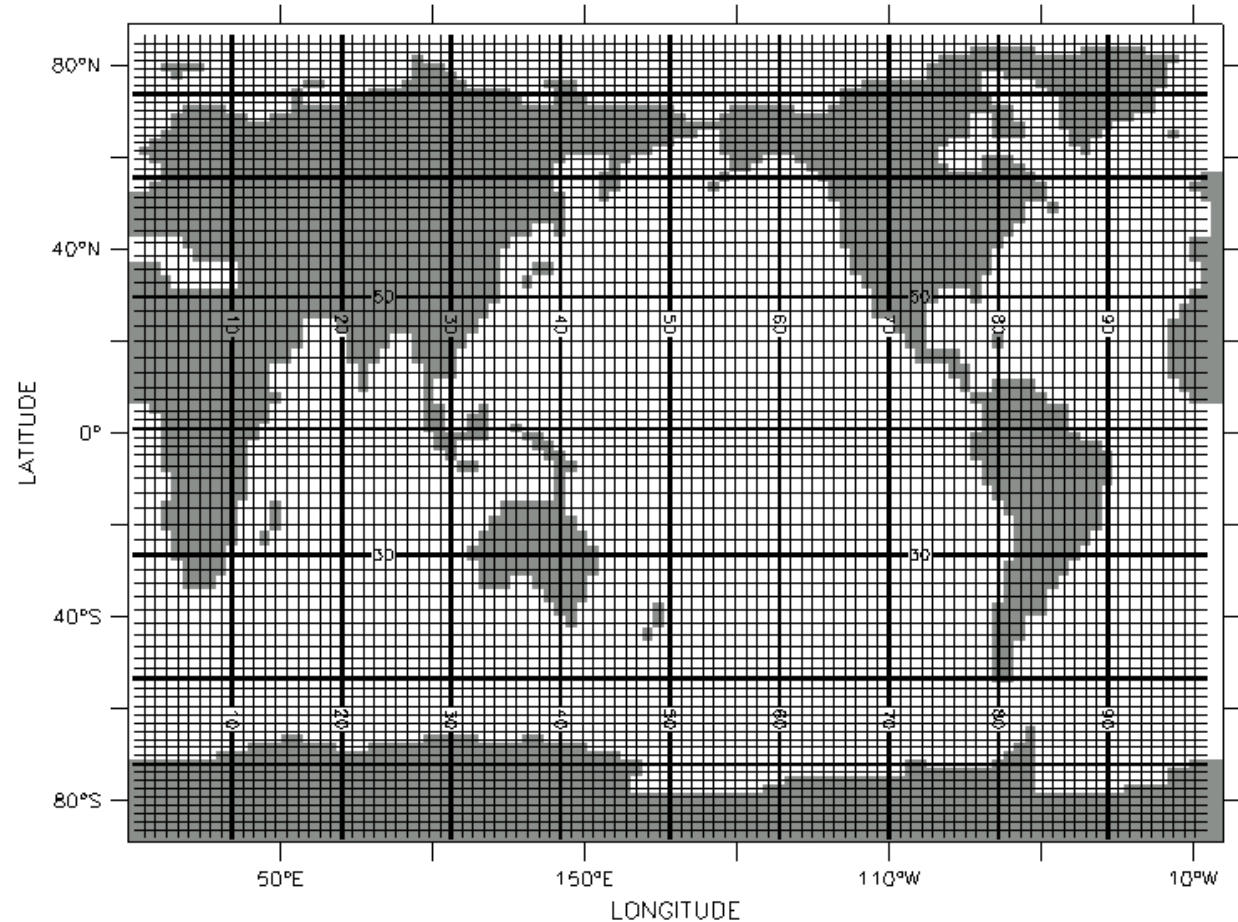
## 1. the horizontal grid

### regular grids:

- are computationally efficient
- have (relatively) straightforward analysis algorithms
- have benefited from decades of research experience

### BUT

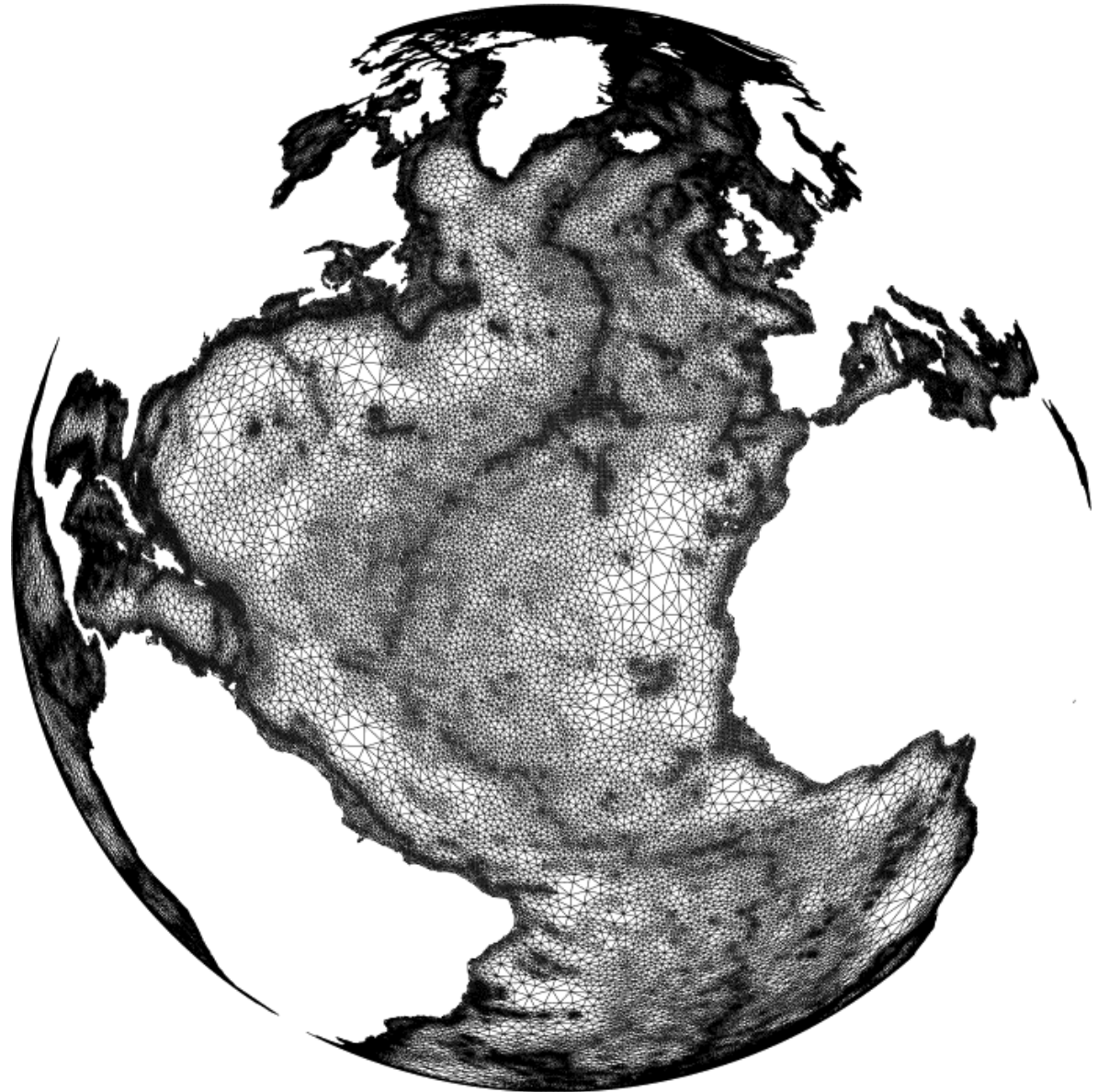
- (for a given latitude) have a fixed resolution: to increase resolution near the edge of an ocean basin (where you want it!) requires an increase of resolution everywhere including out in the middle of the ocean (where you don't!)



# Ocean Model Practicalities I

## 1. the horizontal grid

- **irregular grids** are designed to give you more freedom to put spatial resolution where you want it
- a common scheme is composed as a series of triangles = “**finite elements**”
- by varying the triangle size we can construct a non-uniform horizontal resolution over the computational domain



# Ocean Model Practicalities I

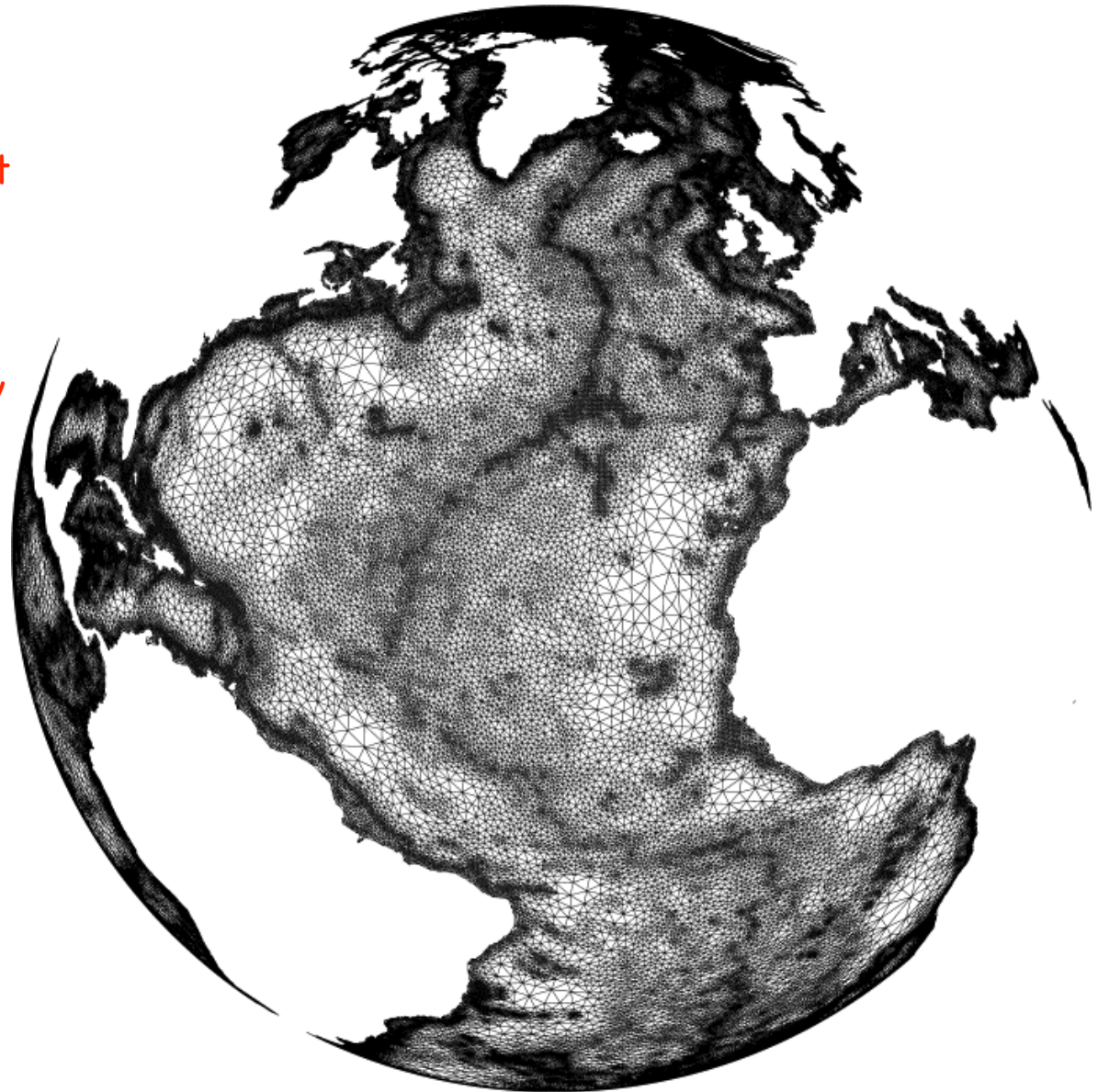
## 1. the horizontal grid

### irregular grids:

- are efficient owing to the fact that resolution can be tailored to need as a function of space
- can accurately represent highly irregular coastlines and topography

### BUT

- are complicated to configure
- have spatially variable resolution-dependent physics (e.g. viscosity and diffusivity coefficients)
- have spatially variable spurious diapycnal mixing
- tools to analyze are immature
- are computationally expensive

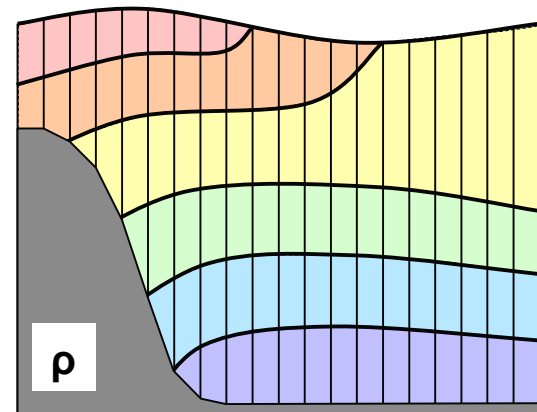
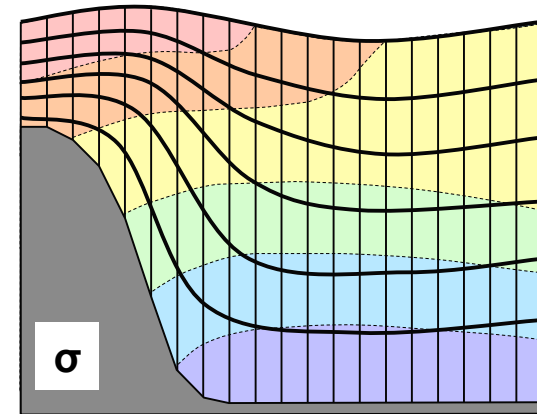
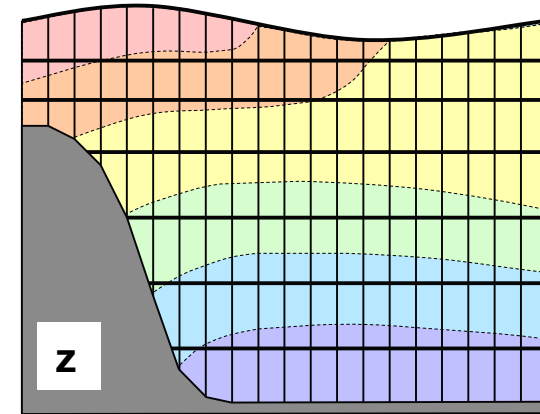




# Ocean Model Practicalities II

## 2. the vertical grid

- the choice of the vertical co-ordinate system is loaded because:
  - the oceans are forced at the surface; most of the “action” occurs there
  - the oceans are strongly stratified
  - the oceans are  $\sim$  adiabatic in the interior
  - there is complex bottom bathymetry to deal with
- as a consequence there exist a number of approaches to choose from





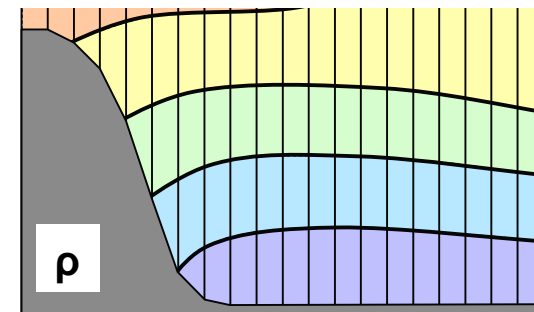
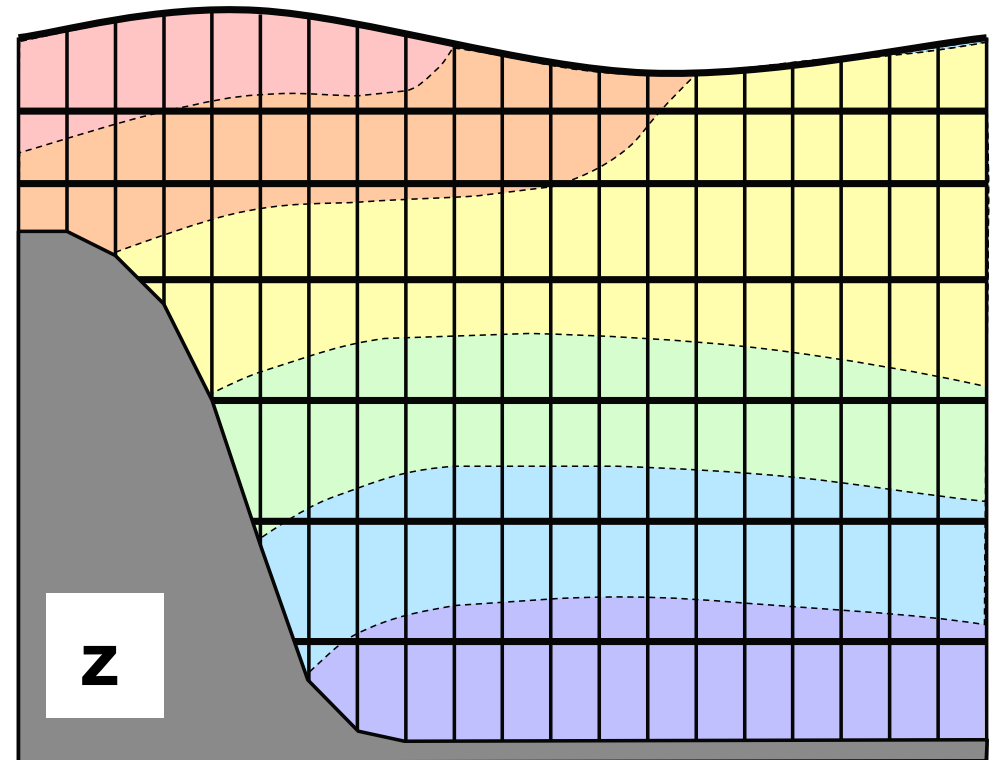
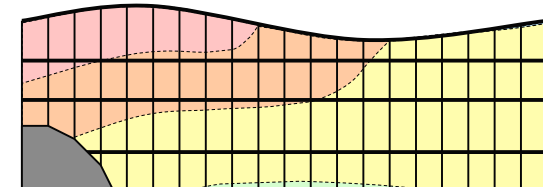
# Ocean Model Practicalities II

## 2. the vertical grid

### 1. absolute depth / z-coordinate system

- based on a series of depth levels
- common to add vertical resolution near the surface by decreasing the spacing between the levels in the upper ocean relative to the deep
- **ADVANTAGES:** simple to set up; computationally efficient; there are no pressure gradient errors
- **DISADVANTAGES:** increased vertical resolution near the lateral boundaries (i.e. on the continental slopes) requires the addition of grid cells throughout the basin; spurious diapycnal mixing associated with the numerical advection scheme

e.g. MOM5 (actually uses  $z^*$ )



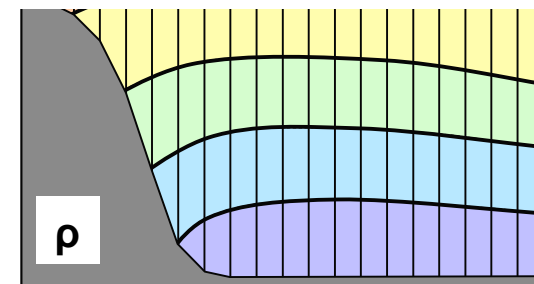
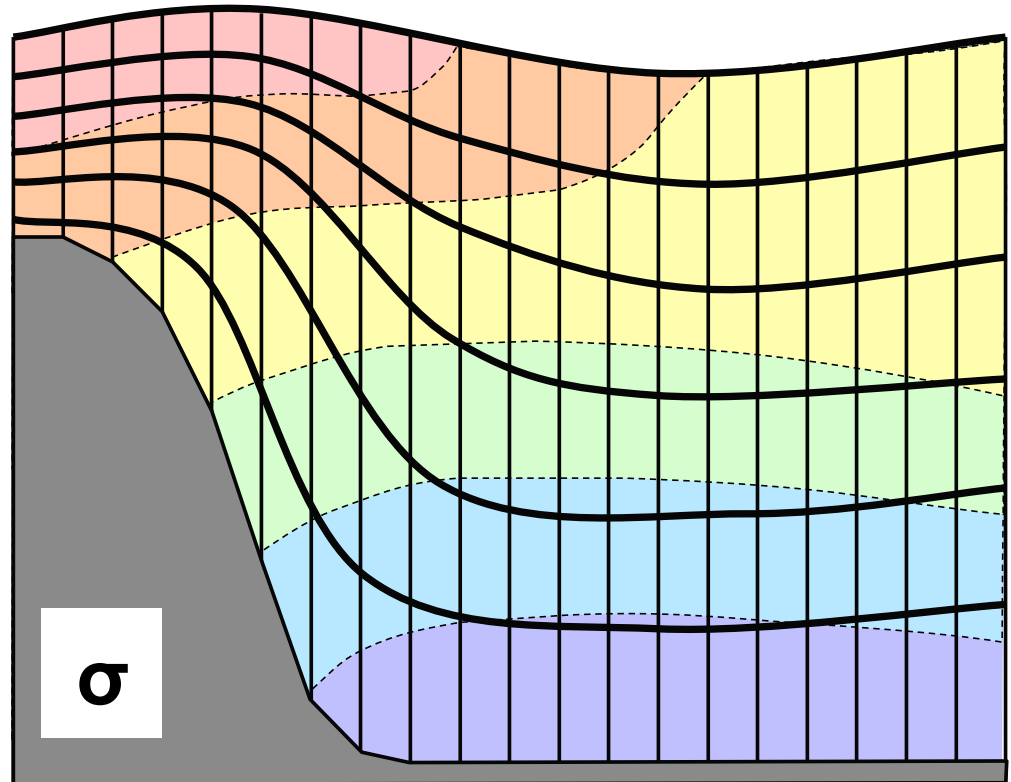
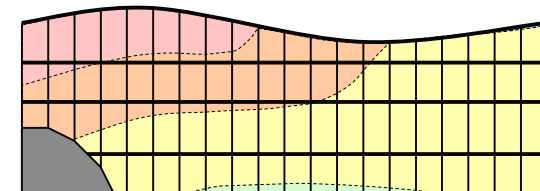
# Ocean Model Practicalities II

## 2. the vertical grid

### 2. “terrain following” / $\sigma$ -coordinate system

- based on the fractional depth, scaled from 0 to 1:
  - $-0.01\sigma$  level is 1% of the depth of the ocean
  - $-0.5\sigma$  level is exactly half the depth of the ocean
  - $-0.99\sigma$  level is at 99% of the depth of the ocean
- **ADVANTAGES:** mimics the bathymetry and allows high resolution near the sea floor regardless of depth or proximity to land
- **DISADVANTAGES:** pressure gradient errors; issues with spurious diapycnal mixing coming from the numerical advection scheme

e.g. ROMS, POM



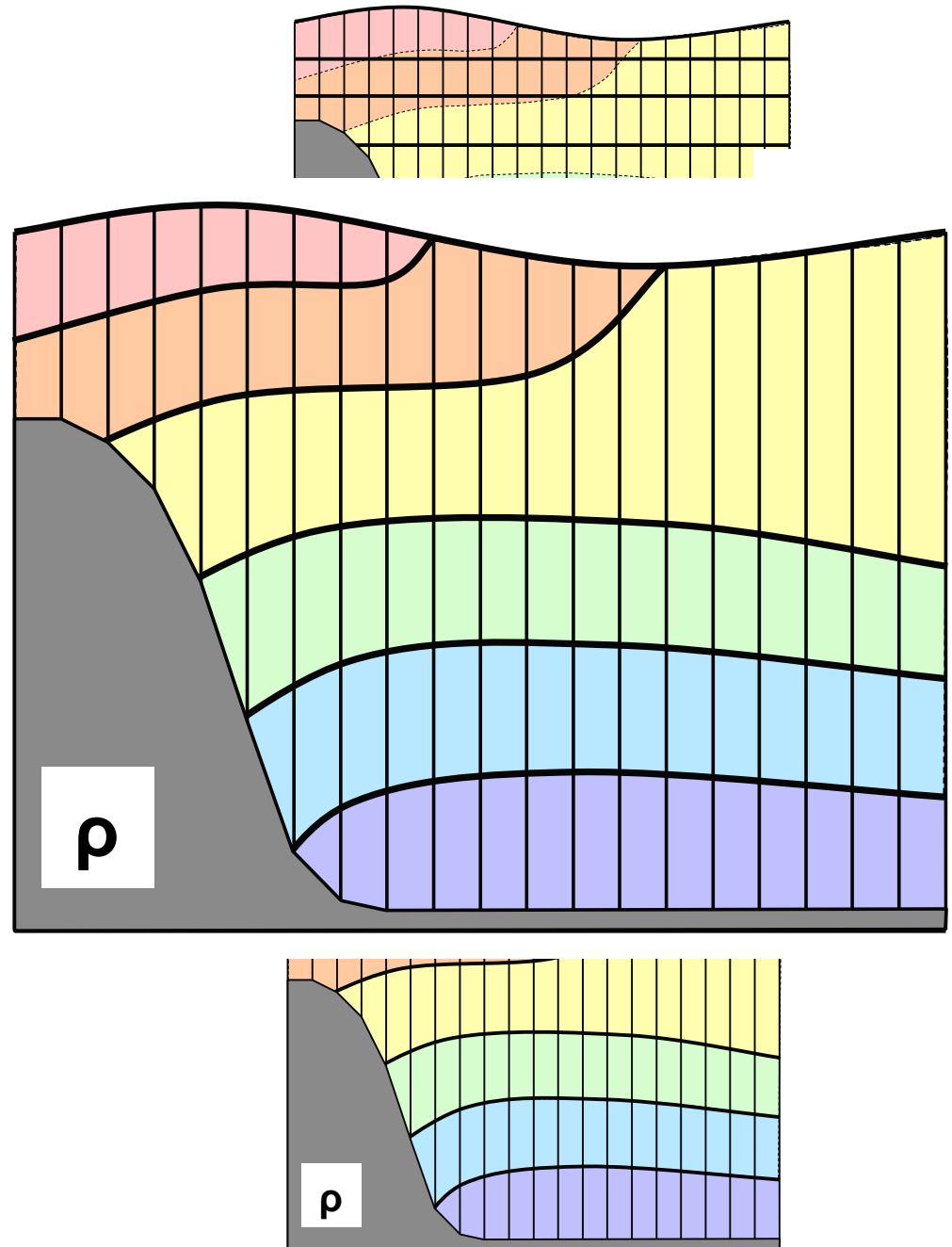
# Ocean Model Practicalities II

## 2. the vertical grid

### 3. density ( $\rho$ ) / “isopycnal” coordinate system (“layered models”)

- vertical grid defined by density surfaces
- exploits the fact that below the mixed layer, ocean currents generally flow along surfaces of equal density (flow is “adiabatic”)
- **ADVANTAGES:** simple, “exactly isopycnal” (no spurious diapycnal mixing!)
- **DISADVANTAGES:** perform poorly where the ocean is less stratified (e.g. in shallow water); no resolution in an unstratified fluid; no mixed layer unless you tack one on; issues with entrainment

e.g. GOLD (precursor to MOM6)



# Ocean Model Practicalities II

## 2. the vertical grid

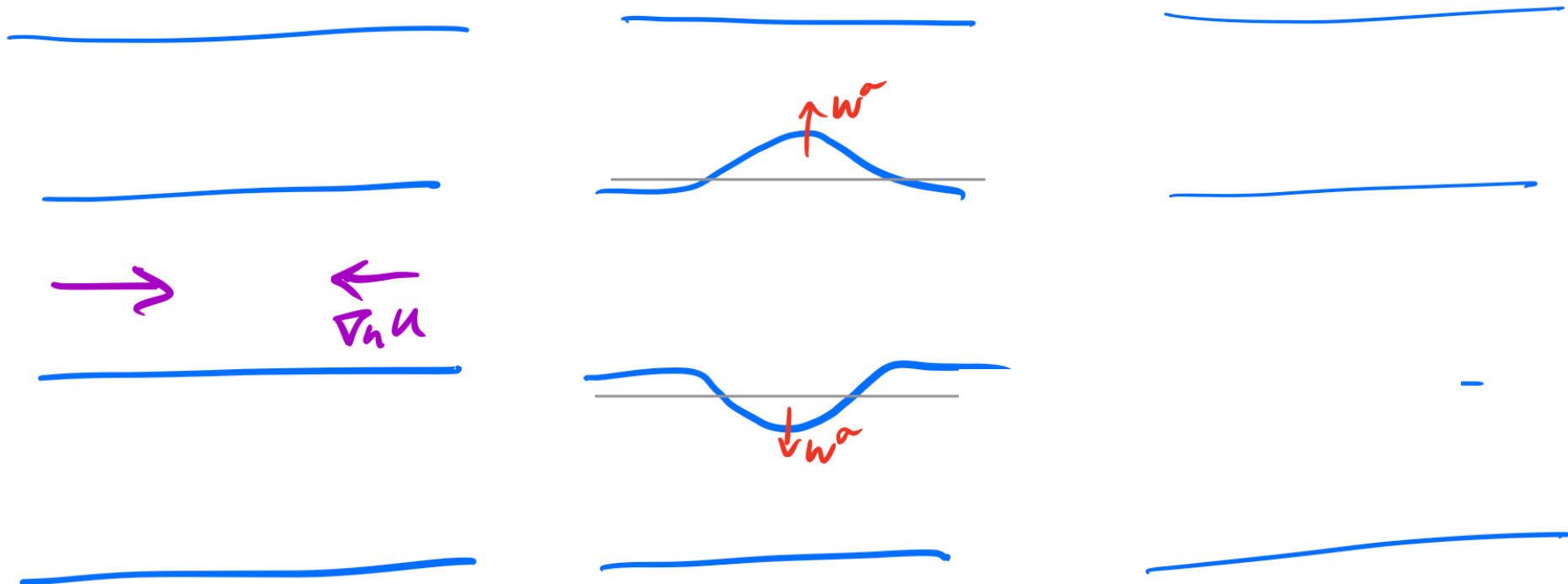
### 4. Arbitrary Lagrangian-Eulerian

- Configurable hybrid system
- Can use  $z$  near surface, terrain-following near bottom and isopycnal interior

**ADVANTAGE:** dynamically optimized coordinate system gives improved results;

**DISADVANTAGE:** it's new!!

e.g. MOM6

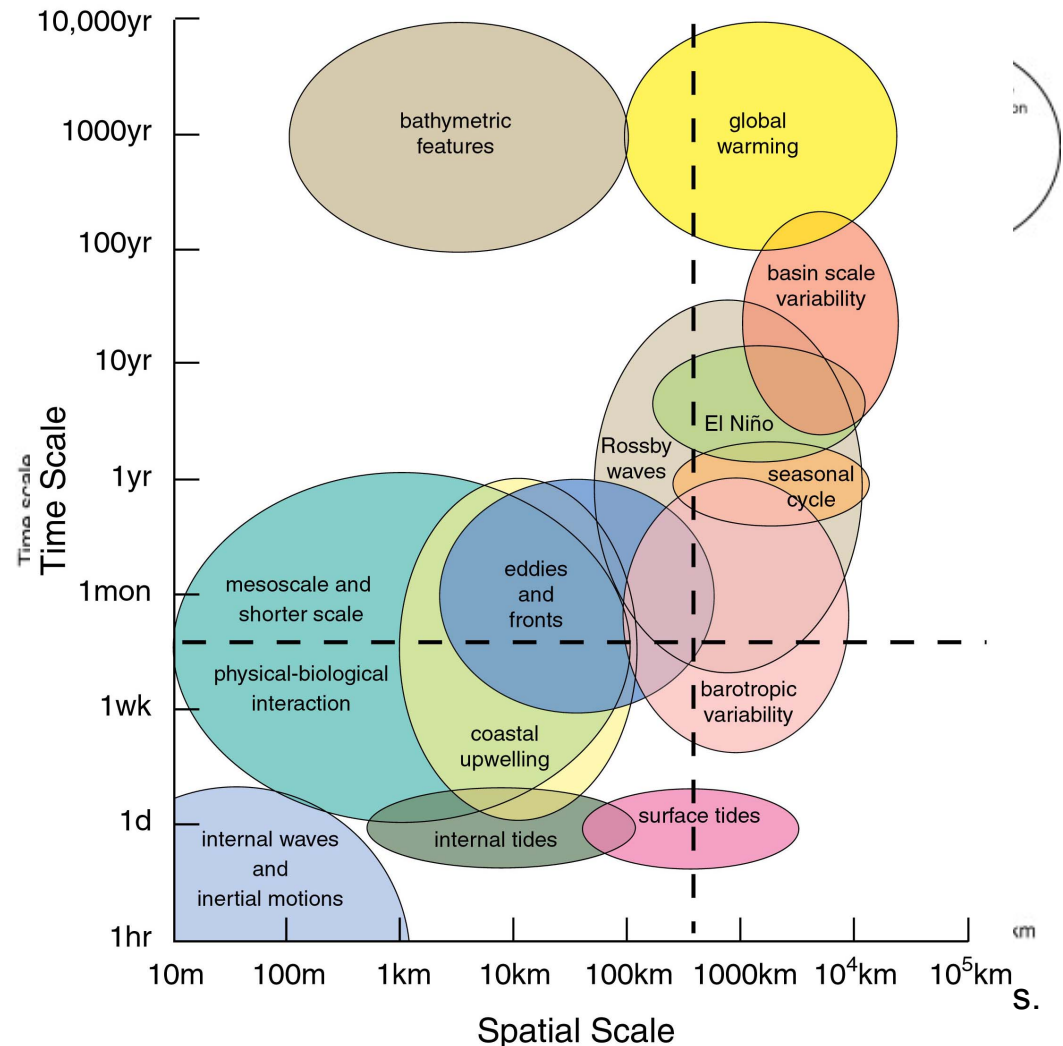


# Ocean Model Practicalities III

## 3. model resolution

### What are we trying to resolve?!?

- like the atmosphere the ocean has “multiple scale variability” = a broadband of time and length scales that are important/on which motions exhibit variation
- further, processes include coupling across scales (“non-local interactions”) and these scale interactions can have important effects
- the range of important time and space scales is immense: molecular (mm and seconds) to basin scale (10 000 km and 1000 years)
- multiple scale variability and scale interactions make ocean dynamics fascinating but very challenging to model!

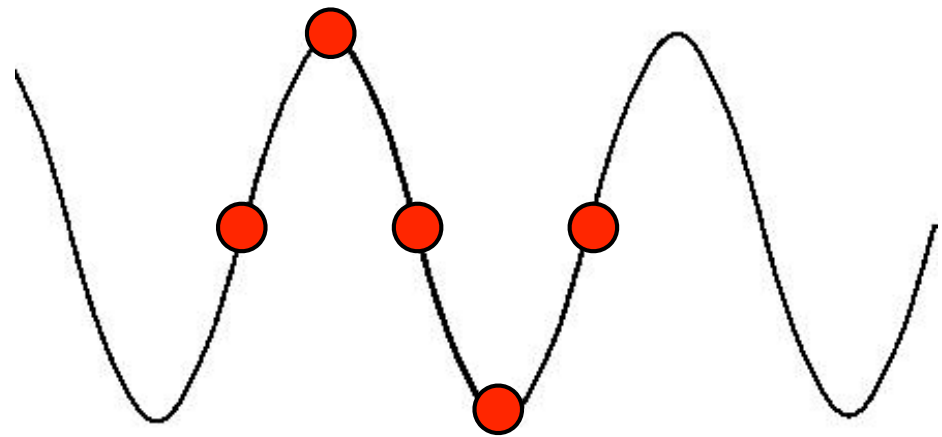




# Ocean Model Practicalities III

## 3. model resolution

- general principles of resolution are the same for both atmospheric and ocean models
- there are different rules of thumb: one is that it takes 5 grid points to accurately define a feature without aliasing
- this means **1/8°** global resolution with an average horizontal grid cell of **14 km** can accurately depict only features larger than **56 km**
- models with variable grid spacing have variable resolution - beware of resolution-dependent physics!
- resolution is not cheap - because of the CFL\* condition, as we shrink the horizontal grid spacing we must add vertical layers and decrease the time step



*"every halving of the grid spacing requires roughly ten times as many computations"*

\* no transport faster than one grid cell per time step!

# Ocean Model Practicalities III

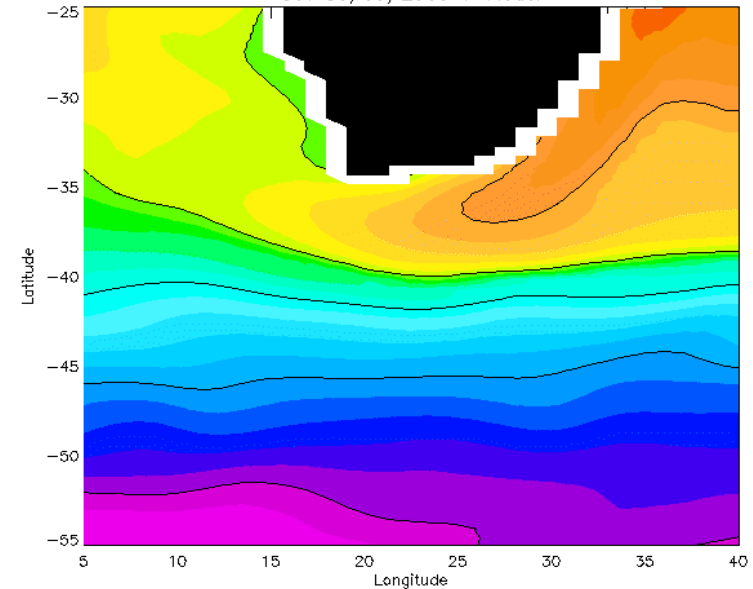
## 3. model resolution

- global ocean models often describe their horizontal resolution with respect to their ability to “permit” or “resolve” mesoscale (i.e. Rossby radius scale) eddies

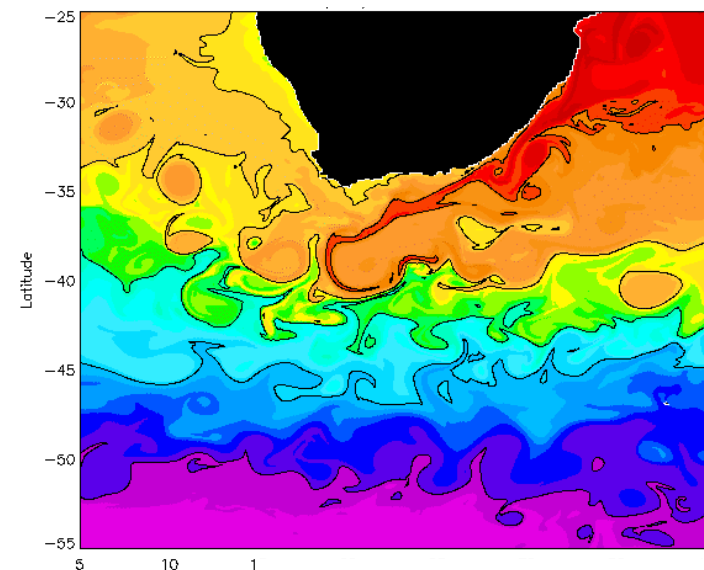
resolution	lingo	meaning
$\geq 1^\circ$	“coarse”	no eddies
$\sim 0.5^\circ$	“eddy-permitting”	some eddies
$\leq 0.2^\circ$	“eddy-rich”	eddies generate at realistic strength and rate

- “eddy rich” does **NOT** mean all eddies are resolved or that all eddy effects of resolved eddies are acting !!!
- the spatial resolution of the ocean component of CMIP5 coupled models is  $0.2^\circ$  to  $2^\circ$ : from “coarse” (no eddies) to “eddy-permitting” (partially resolved eddy field)
- the effects of eddies need to be parameterized in coarse models (more later!); what to do in models that partially resolve the eddy field is an increasingly important question

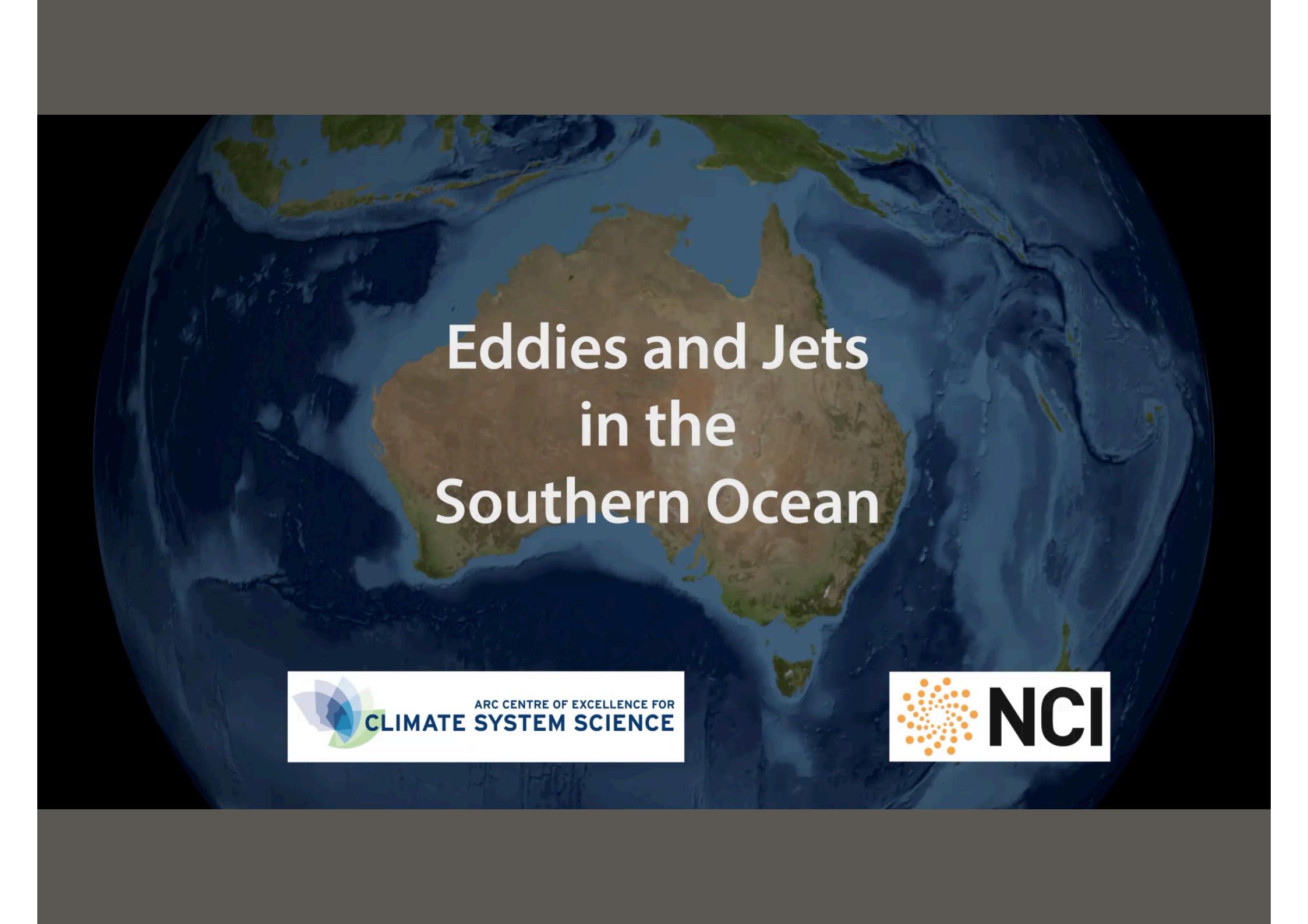
1° “coarse resolution” model



0.1° “eddy-resolving” model



[courtesy of Peter Gent]



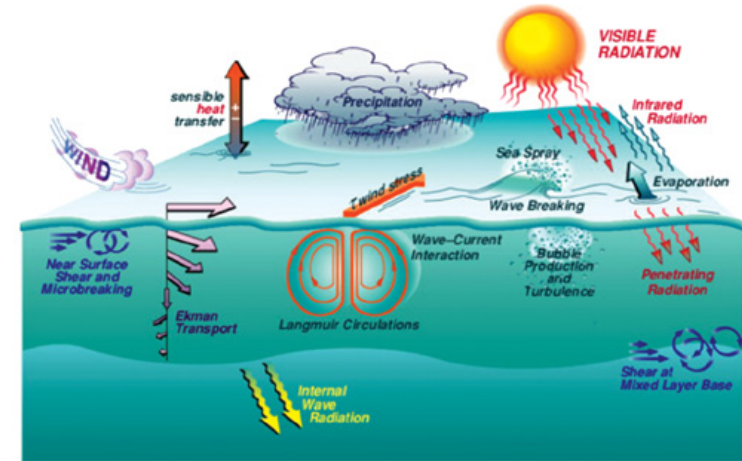
# Eddies and Jets in the Southern Ocean



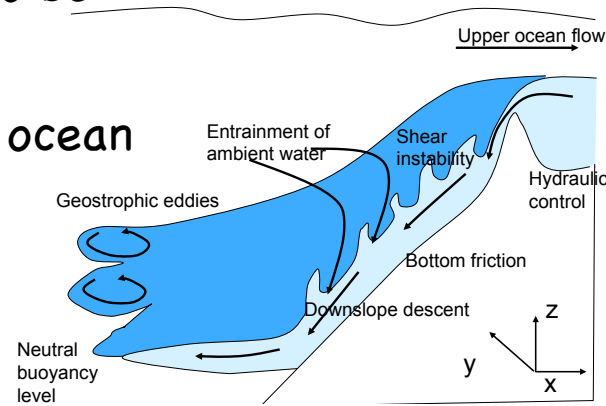
# Ocean Model Practicalities IV

## 4. parameterizations

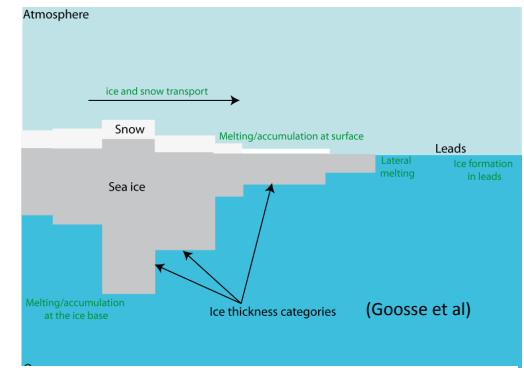
- processes need to be parameterized in a model for 2 main reasons:
  1. we won't spend the computational resources required to directly treat them because they are either too small or too complex;
  2. we don't understand it well enough to be represented by an equation
- processes commonly parameterized in ocean models include:
  - mesoscale eddy effects
  - submesoscale eddy effects
  - dense overflows
  - coastal processes
  - surface mixed layer processes
  - friction
  - sub-grid scale mixing
  - ocean-ice interactions
- low res models: the main problem is mesoscale eddies; high res models: submesoscale eddies (fronts and filaments), internal wave mixing, details of flow-topography interactions



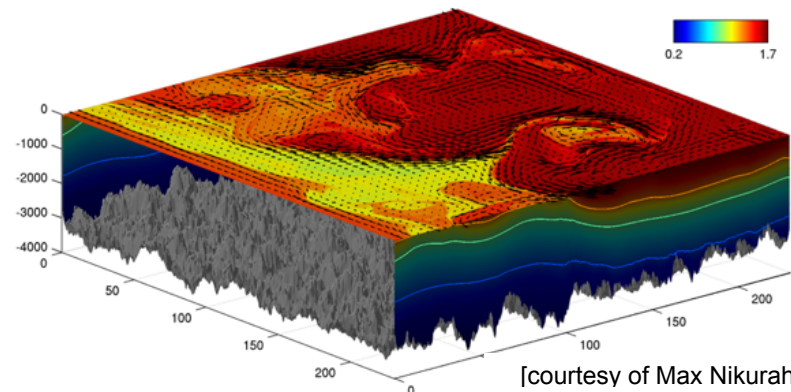
[courtesy of Bob Weller]



[courtesy of Sonya Legg]



[Goosse et al.]



[courtesy of Max Nikurahsin]

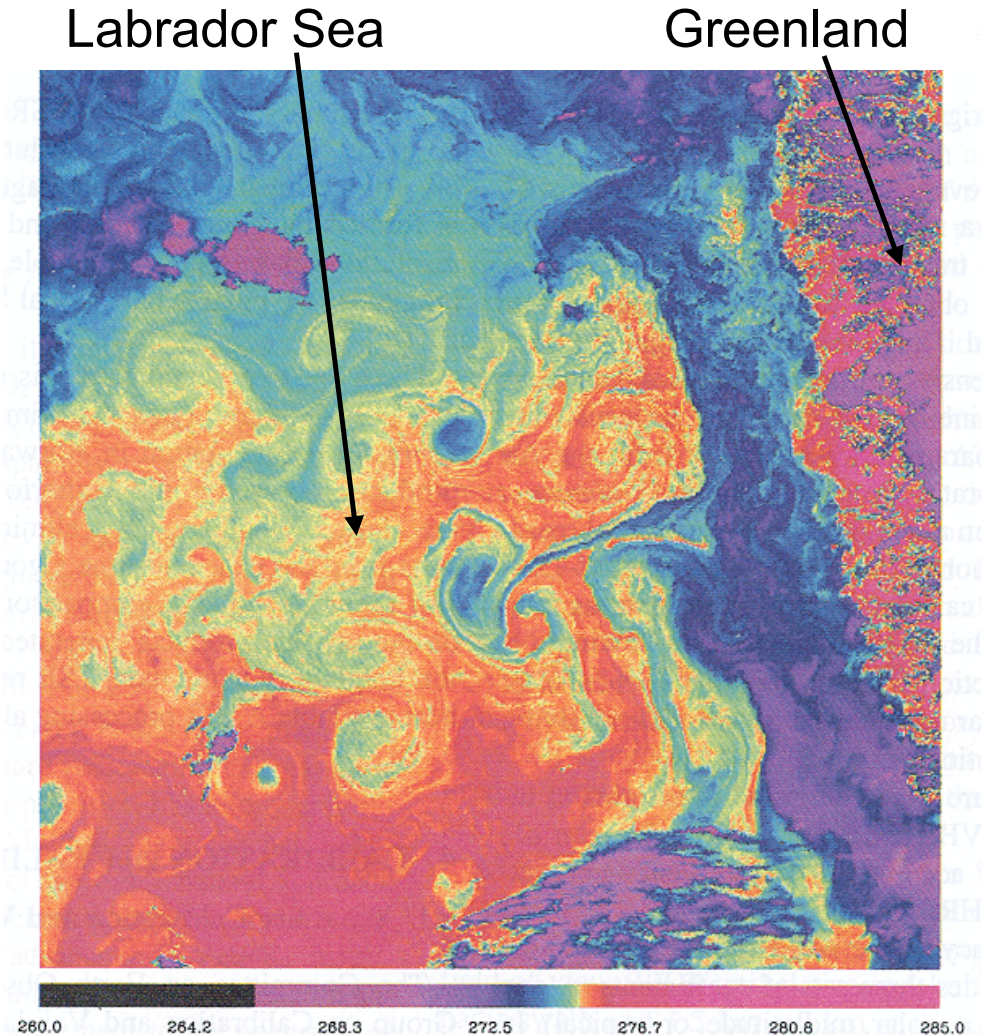


# Ocean Model Practicalities IV

## 4. parameterizations

### 1. parameterizing mesoscale eddy effects:

- mesoscale eddy effects include:
  - mixing along isopycnals
  - restratifying / flattening isopycnals
  - non-local fluxes: transport by rings, Meddies
  - acting as a source of small scale noise/variability
  - modifying air-sea fluxes
  - cascading energy to different scales
  - ...
- **critical** eddy parameterizations in coarse-resolution models are:
  1. **Along-isopycnal diffusion** (Redi)
  2. **Bolus transport** (Gent and McWilliams or "GM")



Sea surface temperature showing the eddy field in the Labrador Sea.



# Ocean Model Practicalities IV

## 4. parameterizations

### 1. parameterizing mesoscale eddy effects:

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  - **mixing along isopycnals**
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  - are a source of small scale noise/variability
  - modify air-sea fluxes
  - cascade energy to different scales
  - ...
- **critical** eddy parameterizations in coarse-resolution models are:

#### 1. Along-isopycnal diffusion (Redi)

= mixing of tracers (temperature, salinity etc.) along density surfaces

2. Bolus transport (Gent and McWilliams or "GM")

$$-\nabla \cdot \langle \vec{u}' \tau' \rangle = \nabla \cdot \kappa_\rho \underline{\underline{K_{Redi}}} \nabla \tau$$

↑
↑
↑

end result of mixing by eddies along density surfaces
isopycnal diffusivity
large-scale (resolved) tracer gradient

where

$$\underline{\underline{K_{Redi}}} = \begin{pmatrix} 1 & 0 & S_x \\ 0 & 1 & S_y \\ S_x & S_y & |S|^2 \end{pmatrix}$$

↑
↑
↑

eddy diffusivity
components of the (resolved) isopycnal slope

[see Redi, 1982]

[courtesy of Sonya Legg]

# Ocean Model Practicalities IV

## 4. parameterizations

### 1. parameterizing mesoscale eddy effects:

- mesoscale eddy effects include:
  - mixing along isopycnals
  - **restratifying / flattening isopycnals**
  - non-local fluxes: transport by rings, Meddies
  - are a source of small scale noise/variability
  - modify air-sea fluxes
  - cascade energy to different scales
  - ...
- **critical** eddy parameterizations in coarse-resolution models are:

1. Along-isopycnal diffusion (Redi)

### 2. Bolus transport (Gent and McWilliams or "GM")

= represents the advective or transport effect of eddies by means of a "bolus" velocity

- mixes "isopycnal thickness" to flatten density surfaces without mixing density (to mimic baroclinic instability)

$$-\nabla \cdot \langle \vec{u}' \tau' \rangle = -\nabla \cdot \langle \tau \rangle \vec{u}^*$$

end result of mixing by the "advective" effect of eddies

$$\vec{u}^* = \begin{pmatrix} u^* \\ v^* \\ w^* \end{pmatrix} = \begin{pmatrix} -\partial_z (\kappa_{GM} S_x) \\ -\partial_z (\kappa_{GM} S_y) \\ \partial_x (\kappa_{GM} S_x) + \partial_y (\kappa_{GM} S_y) \end{pmatrix}$$

"bolus velocity"

components of the (resolved) isopycnal slope

"GM eddy diffusivity"

$$\underline{\underline{\kappa_{GM}}} = \begin{pmatrix} 0 & 0 & -S_x \\ 0 & 0 & -S_y \\ S_x & S_y & 0 \end{pmatrix}$$

[see Gent and McWilliams, 1990]

[courtesy of Sonya Legg]

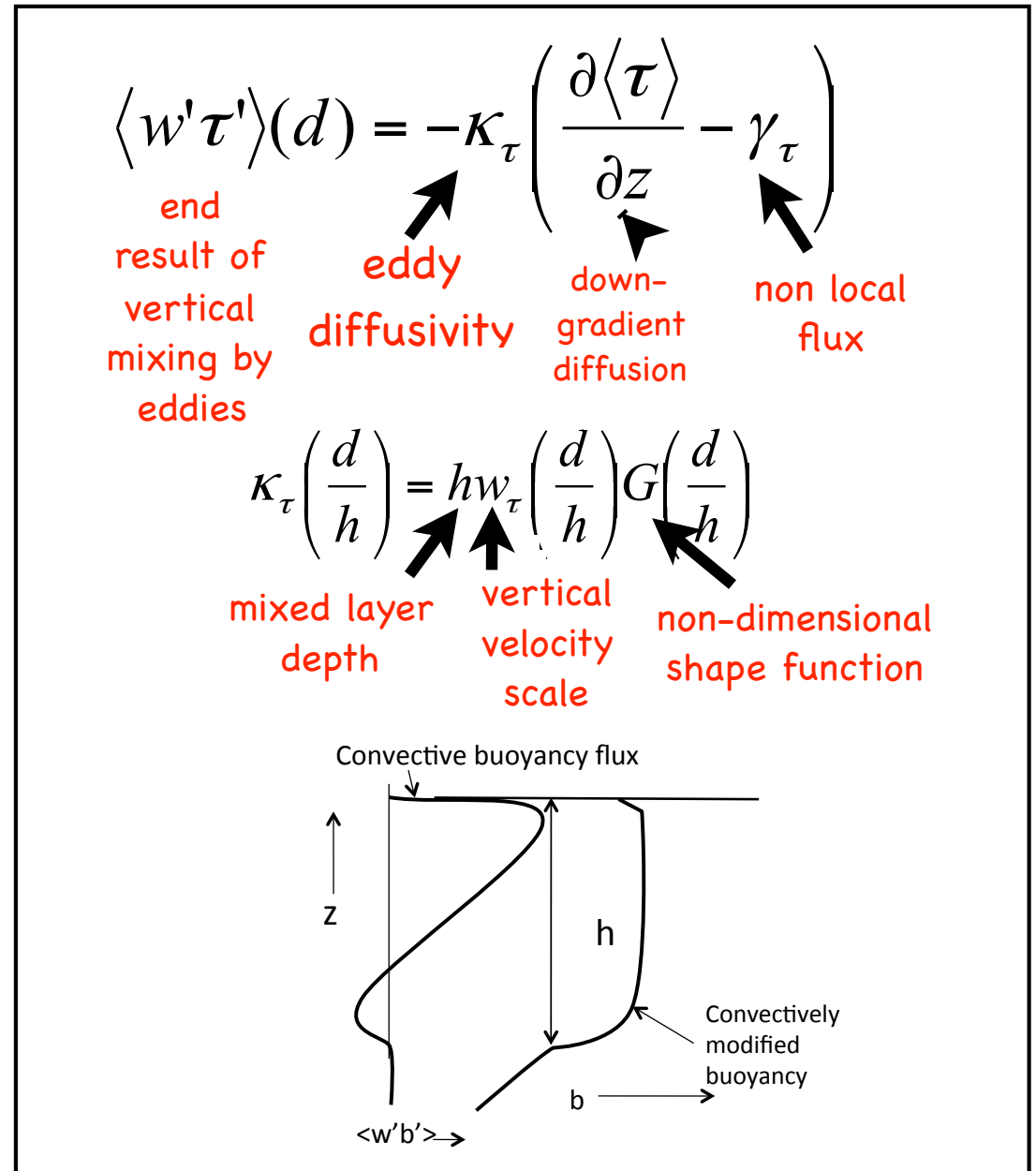
# Ocean Model Practicalities IV

## 4. parameterizations

### 2. vertical mixing schemes

- when the ocean becomes statically unstable ( $\rho_z > 0$ ) vertical over-turning should occur but cannot because we make the hydrostatic approximation (vertical acceleration is excluded!)
- so vertical mixing must be accomplished via a very large coefficient of vertical diffusion
- many models use the **K-Profile Parameterization** (Large et al., 1994)

= large mixing in the upper ocean due to many processes (but dominated by wind) and very much weaker mixing in the deep ocean due to internal wave breaking and tides



# Ocean Models: The Future

**“The ideal ocean climate model has high enough resolution to resolve eddies and topography, zero numerical diffusion and is efficient enough to integrate for 1000s of years.”**

your challenges to solve:

- model biases and model drift
- projections of sea-level rise: most current GCMs are Boussinesq and must calculate the steric contribution to sea-level rise a-posteriori
- the realistic representation of mixing: how much, where? why?
- spurious mixing: models are too diffusive; in z-coordinate resolution models numerical mixing depends on resolution
- overflows
- getting the energy out of the mesoscale eddy field
- sub-mesoscale effects/parameterization
- mixed layer depth and dynamics
- effects of the internal wave field
- parameterizations for partially resolved eddy fields; resolution-dependent parameterizations
- ICE: dynamic ice-sheets and ice shelves, iceberg transport (lack of leads to cold-fresh bias around Antarctica!)
- ...



# Want to know more?

- MIT Open Courseware: “12.984 Atmospheric and Oceanic Modeling”  
<http://ocw.mit.edu/courses/earth-atmospheric-and-planetary-sciences/12-950-atmospheric-and-oceanic-modeling-spring-2004/index.htm>
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